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Principles of Earthquake Forecasting
Short-Term Prediction
Application to Vrancea
apoma Laboratory
Magurele-Bucharest, August 2005

Special day:

Yesterday $M = 3$, Vrancea (one in 5 – 6 days)
(Institute for Earth's Physics Daily Report)

Prediction: Today an $M > 4.8$ (that can be felt in Bucharest), most likely

Probability $\sim 2\%$

Theory validated on the spot!

What means 2% a probability?

Live 50 times the same situation, then you have almost surely one such event!

This means about one $M > 4.8$ surely in one year (50 times 5 – 6 days), in the next day following one of $M > 3$!

Summary

- 1 Principles of Earthquake Forecasting
- 2 Regular Earthquakes. Mean Recurrence Time. Long-Term Forecasting
- 3 Gutenberg-Richter Magnitude Distribution
- 4 Statistical Analysis
- 5 Mean Recurrence Time

Principles of Earthquake Forecasting

-Statistical approach

$$P(M, t, \mathbf{r}, \dots) = d^3N/dMdt\mathbf{r}$$

-A priori knowledge (conditioned probabilities, Bayesian theory)

-Analysis of a statistically significant data set

-Prediction: "what happened will happens again"

-"Shaking" map (effects rate, Mercalli intensity, peak ground acceleration)

$$I(t, \mathbf{r}) = \int dM d\mathbf{r}' I(M, \mathbf{r} - \mathbf{r}') P(M, t, \mathbf{r}')$$

Regular Earthquakes. Mean Recurrence Time. Long-Term Forecasting

(apoLab, 2004-2005)

-Mean recurrence time t_r

-Probability $\sim 1/t_r^2$

-Accumulating seismic energy $t_r \sim E^{1/r}$; geometric exponent $r = 1/3$ (point-like focus)

$r = 1/2$ (two-dimensional fault)

-Gutenberg-Richter $\ln(E/E_0) = bM$ ($b = 3.5$)

Gutenberg-Richter Magnitude Distribution

$$P(M) = \beta e^{-\beta M}, \quad \beta = br$$

-well documented

$$\text{log distr} \quad \ln(N/T) = \ln(\beta \Delta M / t_0) - \beta M$$

$$\text{exced rate} \quad \ln(N_{ex}/T) = -\ln(t_0) - \beta M$$

-seismicity rate $1/t_0 = N_0/T$

Statistical Analysis

-Overall, worldwide data (Bullen, 1963) ($5.8 < M < 7.3$, $\Delta M = 0.1$)

$$\beta = 1.38, (r = 0.39, b = 3.5), 1/t_0 = 10^{5.5} \text{ per year}$$

-Point-like focus model: $\beta = 1.17, (r = 1/3, b = 3.5)$

-California: $\beta = 2.3, r = 0.66, 1/t_0 = 10^{7.5} \text{ per year}$

-Vrancea (apoLab, 2005): $\beta = 1.89, (r = 0.54, \text{fault}), 1/t_0 = 10^{4.21} \text{ per year}$

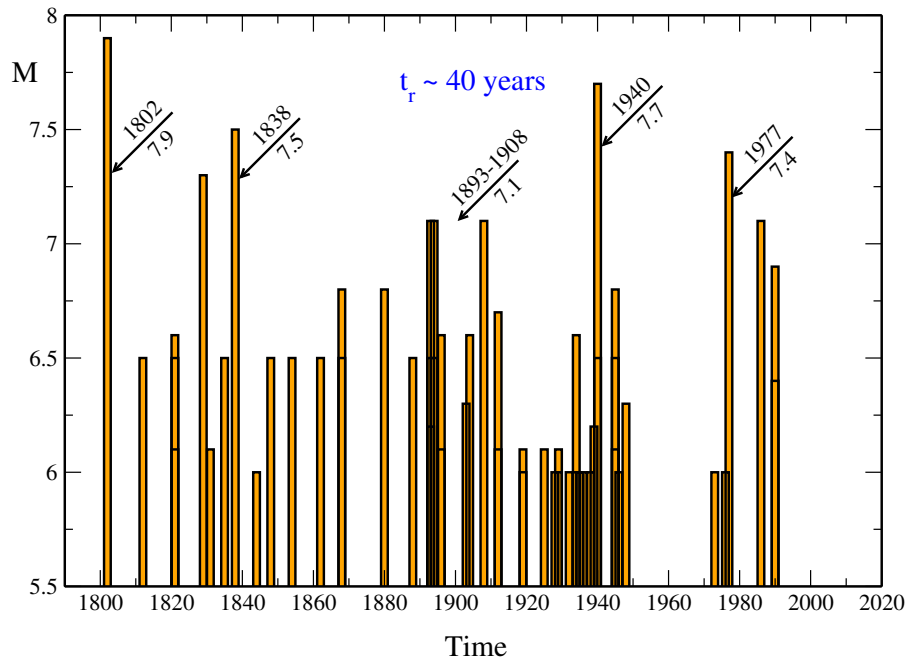
Mean Recurrence Time

$$t_r = (t_0/\beta\Delta M)e^{\beta M}, \quad t_{ex} = t_0e^{\beta M}$$

-Vrancea: $t_r = 34.9 \text{ years } (M > 7)$

-Statistical character, randomness, Poisson assumption $p(t) = t_r e^{-t/t_r}$

-Deviation $(\bar{t}^2)^{1/2} - t_r = 0.41t_r; \quad t_r = 34.9 \pm 14.3 \text{ years; little practical use}$



Vrancea earthquakes with (moment) magnitude $M > 6$ in the last two centuries (Romanian Earthquakes Catalogue, 2005)

Summary

- 1 Accompanying Seismic Activity. Omori's Law
- 2 Short-Term Seismic Activity is More Complex
- 3 California Short-Term Prediction Model

Accompanying Seismic Activity. Omori's Law

(apoLab, 2005)

- Omori's law $dn/d\tau \sim 1/\tau$, aftershocks, or foreshocks
- originating in the self-replication of a generating exponential $\sim e^{-\alpha\tau} = e^{-2\tau/t_r}$
- abrupt fall, long tail
- similar for $m = M_0 - M$; $\sim e^{-\beta|m|}$; $\bar{m} = 0$, $(\bar{m}^2)^{1/2} = \sqrt{2}/\beta = 1.2$ ($\beta = 1.17$); Bath's law
- similar for $1/E$; $dE/d\tau \sim 1/\tau^2$ (emp evidence) ($E \sim 1/\tau$, released energy)

Short-Term Seismic Activity is More Complex

- Omori's law - a particular short-term pattern

$$M = M_0 - \alpha\tau/\beta \quad (\alpha(M_0))$$

- Scarcity of data (poor statistics), little practical use
- Disentangling accompanying events from the regular ones (especially for long time)
- Any aftershock or foreshock: a "main" shock in turn; multi-branch activity
- M and t independent statistical variables

California Short-Term Prediction Model

$$P(M, t, r) = \text{const} \cdot e^{-\beta M} \cdot \frac{1}{t + t_c} \cdot \frac{1}{(r + r_c)^2}$$

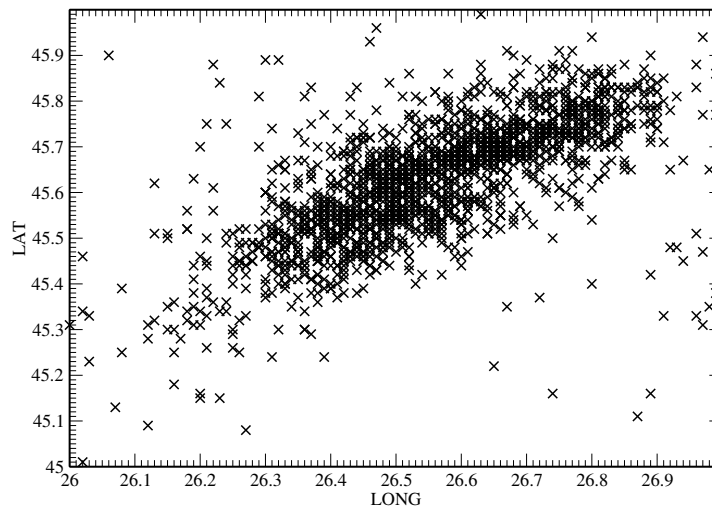
- cutoff t_c , cutoff r_c ; ($t \sim r$; area variables $\rightarrow 1/r^2$); isotropy; spatial grid 5 km

- time-descending sequences, over a few months, within $M \pm 0.5$
- fit; ongoing sequence; prediction; null hypothesis (former half predicts the later half)
- real-time "shaking" map

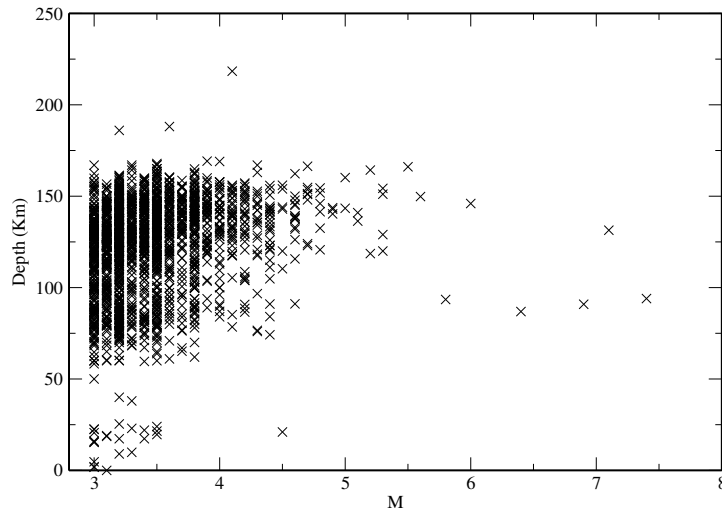
Summary

- 1 Vrancea Focus (Fault)
- 2 Vrancea Earthquakes
- 3 Next-Earthquake Probability $P(t)$, $P(M, t)$
- 4 Time-Magnitude Distribution for the Next-Earthquake $P(t/M_0)$
 $P(M, t/M_0)$
- 5 Next-Earthquake Time-Magnitude Distribution for Threshold Magnitude $M = 4.7$
- 6 Conclusions

Vrancea Focus (Fault)



Geographical distribution of 1999 Vrancea earthquakes with (moment) magnitude $M > 3$ recorded between 1974 and 2004 (30 years) within $45^\circ - 46^\circ\text{N}$ latitude and $26^\circ - 27^\circ\text{E}$ longitude (Romanian Earthquake Catalogue)



Depth distribution of 1999 Vrancea earthquakes with (moment) magnitude $M > 3$ recorded between 1974 and 2004 (30 years) within $45^\circ - 46^\circ\text{N}$ latitude and $26^\circ - 27^\circ\text{E}$ longitude (Romanian Earthquake Catalogue)

Vrancea Earthquakes

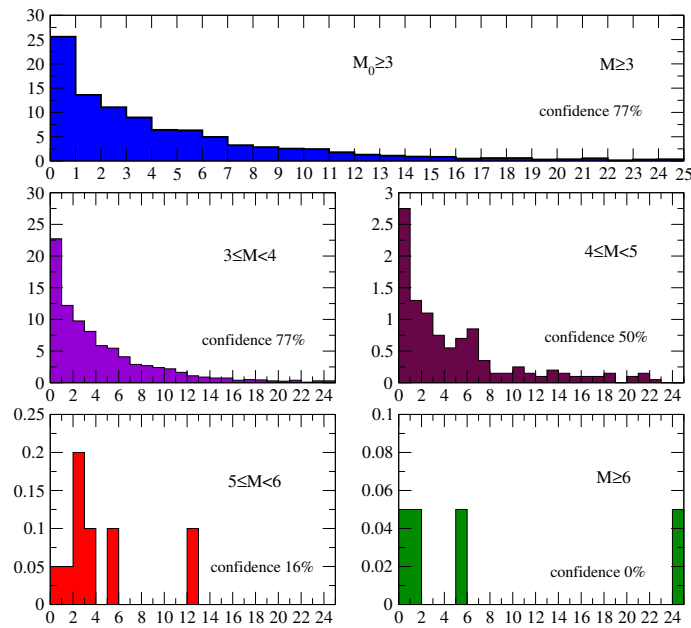
day	N=1998	P(t)%	N($3 < M < 4$)=1769	P($3 < M < 4, t$)%
0	511	25.58	454	22.72
1	272	13.61	244	12.21
2	221	11.06	195	9.76
3	179	8.96	162	8.11
4	128	6.41	117	5.86

N($4 < M < 5$)=211	P($4 < M < 5, t$) %
55	2.75
26	1.30
22	1.10
15	0.75
11	0.55

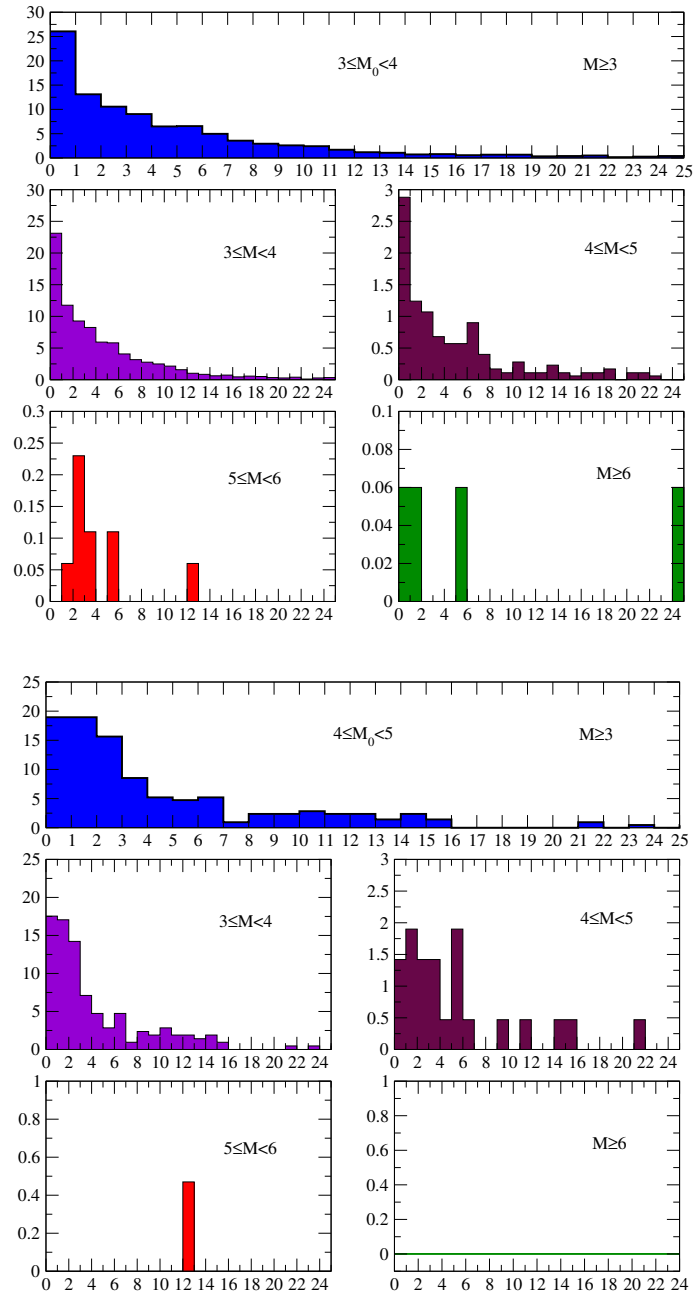
$N(5 < M < 6) = 13$	$P(5 < M < 6, t) \%$	$N(6 < M < 8) = 5$	$P(6 < M < 8, t) \%$
1	0.05	1	0.05
1	0.05	1	0.05
4	0.20	0	0.00
2	0.10	0	0.00
0	0.00	0	0.00

Event distribution for Vrancea next-earthquake (1999 Vrancea earthquakes with (moment) magnitude $M > 3$, recorded between 1974 and 2004 (30 years) within $45^\circ - 46^\circ\text{N}$ latitude and $26^\circ - 27^\circ\text{E}$ longitude (Romanian Earthquake Catalogue)

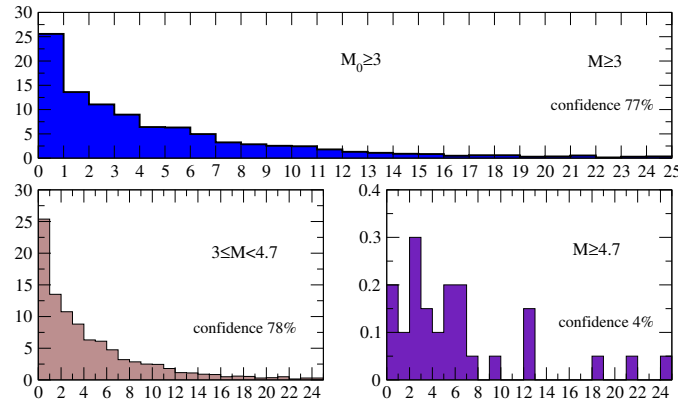
Next-Earthquake Probability $P(t)$, $P(M, t)$



Time-Magnitude Distribution for the Next-Earthquake $P(t/M_0)$, $P(M, t/M_0)$



Next-Earthquake Time-Magnitude Distribution for Threshold Magnitude $M = 4.7$



Conclusions

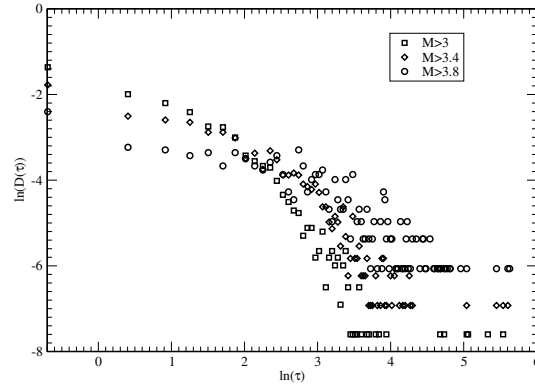
- Decrease in time; Omori- type power laws
- Correlation time $\sim 20 - 25$ days, correlation size $M < 4 - 5$
- Poor statistics for $M > 5$
- Null hypothesis: first half of data to predict the second half of data; confidence level

Summary

- 1 Pair Distribution
- 2 Scaling Time
- 3 Universal Function
- 4 Prediction for Vrancea $M > 5$
- 5 Conclusions

Pair Distribution

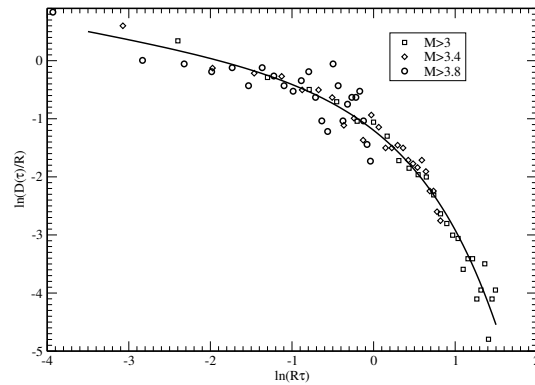
$$D(\tau) = dN/Nd\tau = \frac{1}{N} \sum_i \delta(t_{i+1} - t_i - \tau)$$



Pair distribution vs time (days) for 1999 earthquakes recorded in Vrancea 1974-2004 ($M > 3$)

Scaling Time

$$N = N_{ex} , R = N_{ex}/T = t_0^{-1} e^{-\beta M_c} , D(\tau) = Rf(R\tau)$$



Rescaled pair distributions and the fit (solid curve, $r = 0.25$, $B = 1.17$, $C = 0.71$) for 1999 earthquakes recorded in Vrancea between 1974 and 2004 ($M > 3$)

Universal Function

(apoLab 2005)

- $D(\tau) \sim t \sim E^r \sim 1/\tau^r$; $D(\tau) \sim R/(R\tau)^r$: $R\tau \rightarrow 0$; $r = 0.54$, Vrancea

- $R\tau \gg 1$, exponential, uncorrelated, $D(\tau) \sim e^{-R\tau/B}$

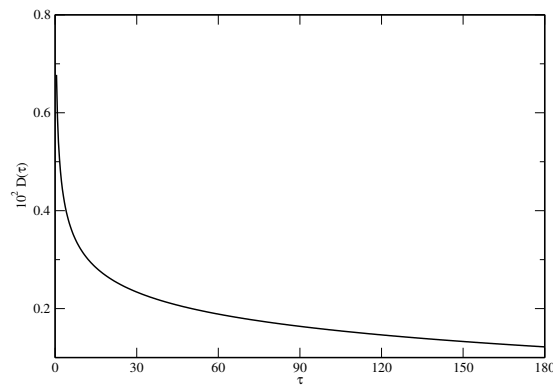
-correction factor $B = R'/R = (1 + e^{bM})^r / e^{brM} \sim 2^r$

-Euler's Gamma class of functions: fitting exponent r

$$D(\tau) = CR \cdot \frac{1}{(R\tau)^r} \cdot e^{-R\tau/B}$$

Prediction for Vrancea $M > 5$

$r = 0.25$, $B = 1.17$, $C = 0.71$ $R = t_0^{-1} e^{-\beta M}$ (fit to recurrence law $\beta = 1.76$, $-\ln t_0 = 8.99$;
actually 18 seisms $M > 5$ out of 1999 in 30 years).



Next-earthquake time (days) distribution for Vrancea $M > 5$

For instance, 0.8% to have two $M > 5$ in the same day

Conclusions

- Main feature of earthquakes: seismicity rate $N_{ex}/T = t_0^{-1}e^{-\beta M}$ (their own rhythm)
- Clustering for small τ ; inverse-power law (both self-replication and Omori's law and regular seismicity); by accumulating energy spatially and releasing it temporaly!
- Randomness for rare events, Poisson-like